

उत्तराखण्ड विद्यालयी शिक्षा परिषद, रू

केन्द्र संख्या की पुनर किन्द्र प्रकरणकार के तन्त्रोदः  
 हाईस्कूल  
 के० सं- 1691

*M. P. Singh*

नोट-केन्द्र के नाम की गृह उत्तरपुरितक के किसी पं भाग पर न लभारं।

परीक्षार्थी द्वारा करा जायेगा

अनुक्रमांक (अंक) में 

2	2	0	4	6	3	4	2
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अनुक्रमांक (शब्दों में) - *Two crore twenty lakh, forty six thousand three hundred forty two*  
 विषय- *Maths*

प्रश्नपत्र संकेतक - 

231
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 (1406)

परीक्षा का दिन - *Tuesday*

परीक्षा तिथि *05 April, 2022*

कक्ष निरीक्षक द्वारा करा जाय-

केन्द्र संख्या - 

1	6	5	1
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परीक्षा कक्ष संख्या 

0	2
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परीक्षा सभी प्रतिप्रिच्छे की जाँच मेरे द्वारा जागान-संपूर्ण कर ली गयी है।

कक्ष निरीक्षक का नाम - *Neena Nautiyal*

दिनांक *05/04/2022*

हरताक्षर कक्ष निरीक्षक *Neena*

परीक्षा किया जाता है कि मैंने इस उत्तरपुस्तिका का मूल्यांकन सम्पन्न कर लेना तथा मूल्यांकन निर्देशों के अनुसार किया है। प्राप्तांकों का मुख्यपत्र पर अधिसारण कर प्राप्तियों एवं प्राप्तांकों के योग का मिलाप कर लिया गया है। एवार्ड ब्लैंक में प्राप्तांकों की अंकन कर उनका पुनः मिलाप भी कर लिया है। किसी भी प्रकार की त्रुटि के लिए मैं उत्तरदायी नहीं रहूँगी।

परीक्षक के हस्ताक्षर एवं संख्या

1. आदेशक के हस्ताक्षर एवं संख्या

2. आदेशक के हस्ताक्षर एवं संख्या

सन्निरीक्षा प्रयोगार्थ

सन्निरीक्षा पूर्व अंक

सन्निरीक्षा पश्चात् अंक-

त्रुटि का प्रकार-

दिनांक-

हरताक्षर निरीक्षक-

Qus. 1 Ans...

⇒ 21

Qus. 2 Ans...

Qus. 3 Ans...

⇒ '616 cm<sup>2</sup>' will be the surface area of sphere whose diameter is 14 cm.

Qus. 4 Ans...

⇒  $\angle B = 90^\circ$

Qus. 5 Ans...

⇒ A die is thrown once, probability of getting an odd no. on the top will be  $\frac{1}{2}$   $\left[\frac{1}{2}\right]$  Answer

Qus. 6 Ans...

⇒ Rational number  $\frac{129}{2^2 \times 5^7 \times 7^5}$  will have non-terminating repeated decimal expansion.

### Qus. 7 Ans...

⇒ Given, sum of zeroes = 0 i.e.  $\alpha + \beta$   
product of zeroes =  $\sqrt{5}$  i.e.  $\alpha\beta$

We know, polynomial:

$$x^2 - (\alpha + \beta)x + \alpha\beta$$

⇒  $x^2 - (0)x + \sqrt{5}$

⇒  $[x^2 + \sqrt{5}]$  is required polynomial

### Qus. 8 Ans...

⇒ Given quadratic equation:

$$x^2 - 4x + 4 = [ax^2 + bx + c] \text{ standard form}$$

To find, nature of roots:

$$\text{Discriminant} = b^2 - 4ac$$

$$\Rightarrow (-4)^2 - 4(1)(4)$$

$$\Rightarrow 16 - 16 = 0$$

∴, in given equation  $b^2 - 4ac = 0$ ,  
therefore, the quadratic equation  
( $x^2 - 4x + 4 = 0$ ) will have two  
equal roots.

Qus. 9 Ans...

⇒ A circle can have infinitely many tangents.

Qus. 10 Ans...

⇒ Probability of a sure event is '1'

Qus. 11 Ans...

⇒ Let the larger number be 'x'  
and smaller no. be 'y'  
∴ [such that  $x > y$ ].  
Then, according to question,

$$x - y = 26 \quad \rightarrow \textcircled{1}$$

Also, given, larger no. is three times the smaller

$$\Rightarrow x = 3y \quad \rightarrow \textcircled{2}$$

Putting this value in eq<sup>n</sup> ①, we get

$$\Rightarrow 3y - y = 26$$

$$2y = 26$$

$$\Rightarrow [y = 13] \text{ Sol}^n$$

On putting 'y = 13' in eq<sup>n</sup> ②, we obtain

$$[x = 3 \times 13 = 39] \text{ Sol}^n$$

Therefore, the two numbers are  
39 & 13

### Qus 12. Ans...

$$\Rightarrow \text{Given, } \cos \theta = \frac{4}{5}$$

We know,  $\cos \theta = \frac{\text{Base}}{\text{Hypotenuse}}$

$$\Rightarrow \frac{\text{Base}}{\text{Hypotenuse}} = \frac{4k}{5k} \quad \therefore \text{Base} = 4k$$
$$\text{Hypotenuse} = 5k$$

Such that, 'k' is any +ve integer

Then, according to pythagorean theorem

$$(\text{Hypotenuse})^2 = (\text{Base})^2 + (\text{Perpendicular})^2$$

$$\Rightarrow (5k)^2 = (4k)^2 + (P)^2$$

$$\Rightarrow P = \sqrt{25k^2 - 16k^2}$$

$$P = \sqrt{9k^2} = 3k$$

or we can say:

$$\text{Perpendicular} = 3$$

Now, given,  $(\cot \theta + \operatorname{cosec} \theta)^2$

$$\therefore \cot \theta = \frac{\text{Base}}{\text{Perpendicular}} = \frac{4k}{3k}$$

$$\operatorname{cosec} \theta = \frac{\text{Hypotenuse}}{\text{Perpendicular}} = \frac{5k}{3k}$$

$$\Rightarrow \left( \frac{4k}{3k} + \frac{5k}{3k} \right)^2 = \left( \frac{9k}{3k} \right)^2 = (3)^2 = \boxed{9} \text{ Answer}$$

### Qus. 13 Ans...

$\Rightarrow$  Given, coordinates: let ~~ABC~~  $A$  &  $B$

$$A = (3, 2)$$

$$B = (-2, -3)$$

$$C = (2, 3) \text{ Using distance formula:}$$

$$\text{i.e. } \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

$\therefore$   
We get,

$$AB = \sqrt{(-2-3)^2 + (-3-2)^2}$$

$$\Rightarrow \sqrt{(5)^2 + (5)^2} = \sqrt{25 + 25} = \sqrt{50} \text{ unit}$$

$$BC = \sqrt{(2+2)^2 + (3+3)^2}$$

$$\Rightarrow \sqrt{(4)^2 + (6)^2} = \sqrt{16 + 36} = \sqrt{52} \text{ unit}$$

$$AC = \sqrt{(2-3)^2 + (3-2)^2}$$

$$\Rightarrow \sqrt{(-1)^2 + (1)^2} = \sqrt{1+1} = \sqrt{2} \text{ unit}$$

Here,  $AB + BC > AC$

i.e.  $\sqrt{50} + \sqrt{52} > \sqrt{2}$

Also, Vice-versa,

Since, sum of any two sides is greater than third side,  $\therefore$  these coordinates can form a triangle. (Yes)

Triangle is ~~an~~ triangle because

### Qus 14. Ans ....

⇒ In provided figure,  $\triangle ABC$  has  
 $DE \parallel AC$ .

Then, by using Basic Proportionality  
Theorem:

$$\frac{AD}{BD} = \frac{CE}{BE}$$

$$\Rightarrow \frac{3}{3} = \frac{4}{x} \Rightarrow 3x = 12$$

$$\Rightarrow x = \frac{12}{3} = \boxed{4} \text{ Ans}$$

Therefore, we obtain  $x = 4$ .

### Qus. 15 Ans...

(a) ⇒ To find probability of drawing  
an ace card from well shuffled  
deck of 52 cards;  $P(E)$ .

We know,

total possible outcome = 52; as there  
are total 52 cards.

Also, there are total 4 set in a  
deck, each set has one ace.

i.e. ⇒  $P(E) = \frac{\text{total favourable outcome}}{\text{total possible outcome}}$

$$\Rightarrow P(E) = \frac{4}{52} = \left[ \frac{1}{13} \right] \text{ Ans}$$

(b)  $\Rightarrow$  a red card.

Then Out of 4 deck set in a deck, 2 sets  
are <sup>of</sup> red cards each of 13 cards  
<sub>count</sub>

$\therefore$  Total red cards in a deck =  $2 \times 13$   
= 26

$\therefore$  Hence,  $P(E) = \frac{26}{52} = \left[ \frac{1}{2} \right]$  Ans

Qus. 16 Ans...

$\Rightarrow$  We need to prove  $\sqrt{7}$  is irrational

Let us assume  $\sqrt{7}$  is rational  
[By proof of contradiction]

Then,  $\sqrt{7}$  can be written in the form  
 $p/q \Rightarrow \sqrt{7} = \frac{p}{q}$

[If we ~~use~~  $p$  &  $q$  have common factor other  
than 1, then we can divide  $p$  &  $q$  by  
that no.]

Thus we have  $p$  &  $q$  as co-prime

$\Rightarrow \sqrt{7} = \frac{p}{q} \quad (q \neq 0)$

$q\sqrt{7} = p$



$$7q^2 = p^2 \rightarrow \textcircled{1}$$

$\Rightarrow$  This shows that  $p^2$  is divisible by 7, and if  $p^2$  is divisible then  $p$  will also be divisible by 7 (by theorem)

Now, let,  $p = 7a$

Then, eq<sup>n</sup> 1 become,  
 $7q^2 = (7a)^2$

$$\Rightarrow 7q^2 = 49a^2$$

$$\Rightarrow q^2 = 7a^2 \rightarrow \textcircled{2}$$

This shows that  $q^2$  is divisible by 7, and same  $q$  also

From above, eq<sup>n</sup>s we obtain,

"7" as common factor of  $p$  &  $q$   
But this contradicts to fact that they are co-prime

This contradiction has arisen due to our false assumption,

Hence, our assumption is false, thus, we can conclude that  $\sqrt{7}$  is irrational.

### Qus. 17 Ans...

⇒ Given, quadratic equation; (has equal roots)

$$(a-12)x^2 + 2(a-12)x + 2 = 0$$

To find value of 'a'

Since, equation has two equal roots ⇒

$$b^2 - 4ac = 0$$

$$\text{Here, } b = 2(a-12) = 2a-24$$

$$a = a-12$$

$$c = 2$$

Thus we can write,

$$(2a-24)^2 - 4(a-12)(2) = 0$$

$$\text{i.e. } (4a^2 + 576 - 96a) - 8a + 96 = 0$$

$$\Rightarrow 4a^2 + 672 - 104a \quad \text{or} \quad 4a^2 - 104a + 672$$

Dividing eq<sup>n</sup> by '4'

$$\Rightarrow a^2 - 26a + 168 = 0$$

$$\Rightarrow a^2 - 12a - 14a + 168 = 0$$

$$\Rightarrow a(a-12) - 14(a-12) = 0$$

$$\Rightarrow (a-12)(a-14) = 0$$

$$\begin{array}{l} \text{for, } a-12=0 \quad ; \quad [a=12] \\ \text{for, } a-14=0 \quad ; \quad [a=14] \end{array} \quad \underline{\underline{AM}}$$

The pre. value of 'a' can be either 12  
or 14

## [Qus. 18 Ans.]

⇒ Given, equations:

$$\frac{1}{x} + \frac{2}{y} = 3 \rightarrow \textcircled{1} \text{ eq}^n$$

$$\frac{2}{x} - \frac{4}{y} = 2 \rightarrow \textcircled{2} \text{ eq}^n$$

Let,  $\frac{1}{x} = A$  &  $\frac{1}{y} = B$

Then, eq<sup>n</sup> 1 becomes, ⇒  $A + 2B = 3 \rightarrow \textcircled{3} \text{ eq}^n$   
& eq<sup>n</sup> 2 " ⇒  $2A - 4B = 2 \rightarrow \textcircled{4} \text{ eq}^n$

Multiplying 2 with eq<sup>n</sup> ③

⇒  $2A + 4B = 6 \rightarrow \textcircled{5} \text{ eq}^n$

On solving eq<sup>n</sup> 4 & 5, (elimination method)  
we obtain  $\left[ B = \frac{1}{2} \right]$

on putting this value in eq<sup>n</sup> 3,

we get,  $A + 1 = 3$   
⇒  $A = 2$

Hence, we have  $A = 2$  &  $B = \frac{1}{2}$

Now, we have:  $A = \frac{1}{x} = 2 \Rightarrow x = \left[ \frac{1}{2} \right] \underline{\underline{\text{Ans}}}$

Similarly:  $B = \frac{1}{y} = \frac{1}{2} \Rightarrow y = \left[ 2 \right] \underline{\underline{\text{Ans}}}$

### Qus. 19 Ans.

⇒ Given, first term of an A.P. = 5  
Last term same A.P. = 45

$$\Rightarrow a = 5, (a_n) = 45$$

Also, given, Sum of terms,  $S_n = 400$

$$\Rightarrow S_n = \frac{n}{2} [a + l]$$

$$\Rightarrow 400 = \frac{n}{2} [5 + 45]$$

$$\Rightarrow \frac{50n}{2} = 400 \Rightarrow n = \frac{400 \times 2}{50}$$

$$n = \frac{800}{50} = [16] \text{ Ans}$$

To find common difference,

$$a_{16} = a + (16-1)d$$

$$\Rightarrow 45 = 5 + 15d$$

$$\Rightarrow \frac{40}{15} = d \Rightarrow d = \left[ \frac{8}{3} \right] \text{ Ans}$$

Therefore, we obtain, total number of terms in A.P. = 16

and common difference of A.P. =  $\left[ \frac{8}{3} \right]$

### [ Qus. 20 Ans. ]

$$\Rightarrow \text{To prove: } 1 + \sec A = \frac{\sin^2 A}{1 - \cos A}$$

Taking L.H.S.

$$\Rightarrow \frac{1 + \sec A}{\sec A} = \frac{1}{\sec A} + \frac{\sec A}{\sec A}$$

$$\Rightarrow \cos A + 1 \text{ or } [1 + \cos A] \text{ LHS}$$

Taking R.H.S

$$\Rightarrow \frac{\sin^2 A}{1 - \cos A} \quad [\because \sin^2 A = 1 - \cos^2 A]$$

$$\Rightarrow \frac{1 - \cos^2 A}{1 - \cos A} \quad [\because (1)^2 - \cos^2 A = (1 + \cos A)(1 - \cos A)]$$

$$\Rightarrow \frac{(1 + \cos A)(1 - \cos A)}{1 - \cos A} = [1 + \cos A] \text{ R.H.S}$$

We get,  $1 + \cos A = 1 + \cos A$

$$\Rightarrow \text{L.H.S} = \text{R.H.S}$$

Hence proved!

### Ques. 21 Ans...

$\Rightarrow$  Given coordinates  $A(-1, 7)$  &  $B(4, -3)$  forming a line segment,

Let a line segment = AB

\* Let  $(x, y)$  be the coordinate which

divides AB in the ratio 2:3

Thus,  $m_1 : m_2 \Rightarrow 2 : 3$

Then, by using section formula, <sup>for</sup>  $(x, y)$

$$x = \left[ \frac{m_1(x_2) + m_2(x_1)}{m_1 + m_2} \right]$$

$$y = \left[ \frac{m_1(y_2) + m_2(y_1)}{m_1 + m_2} \right]$$

$$\Rightarrow x = \left[ \frac{2(4) + 3(-1)}{2+3} \right] \Rightarrow \frac{8-3}{5} = \frac{5}{5} = \boxed{1}$$

$$\Rightarrow y = \left[ \frac{2(-3) + 3(7)}{2+3} \right] \Rightarrow \frac{-6+21}{5} = \frac{15}{5} = \boxed{3}$$

∴, required coordinate  $(x, y) = (1, 3)$   
Solution

[ Qus. 22 Ans... ]

⇒ Given, a point on  $x$ -axis which is equidistant from  $(2, -5)$  &  $(-2, 9)$

Let, that point be  $P(x, y)$  ⇒ since it lies on  $x$ -axis ⇒  $(x, 0)$  i.e.  $P = (x, 0)$

Let,  $A = (2, -5)$  &  $B = (-2, 9)$

According to question,

$$AP = BP \rightarrow \textcircled{1}$$

Using distance formula:

$$\sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

$$\text{eq(1)} \Rightarrow \sqrt{(2-x)^2 + (-5-0)^2} = \sqrt{(-2-x)^2 + (9-0)^2}$$

On squaring both sides

$$\Rightarrow (2-x)^2 + (-5)^2 = (-2-x)^2 + (9)^2$$

$$\Rightarrow 4 + x^2 - 4x + 25 = 4 + x^2 + 4x + 81$$

$$\Rightarrow -4x - 4x = 81 - 25$$

$$-8x = 56$$

$$x = \frac{56}{-8} = [-7]$$

Therefore required coordinate  $(x, 0) = [(-7, 0)]$

[ Qus. 23 Ans... ]

$\Rightarrow$  In the provided figure:

side of square ABCD = 14 cm

Then, its area = Side  $\times$  side

$$= 14 \times 14$$

$$\text{Area of square} = [196 \text{ cm}^2]$$

$$\text{Area of semicircle} = \frac{1}{2} \times \pi \times (r)^2$$

In the given semicircle, radius = half of side of square =  $\frac{14}{2} = 7 \text{ cm}$

$$\text{Therefore area of semi-circle} = \frac{1}{2} \times \frac{22}{7} \times 7 \times 7$$

$$\Rightarrow \underline{77 \text{ cm}^2}$$

$$\begin{aligned} \text{Then, area of 2 semi circle} &= 2 \times 77 \text{ cm}^2 \\ &= [154 \text{ cm}^2] \end{aligned}$$

It is clear from fig. that :

$$\begin{aligned} \text{Area of shaded region} &= (\text{Area of square}) \\ &\quad - (\text{area of } 2 \times \text{semi circles}) \end{aligned}$$

$$\Rightarrow \text{Area of shaded region} = 196 - 154$$

$\Rightarrow \underline{42 \text{ cm}^2}$  Solution

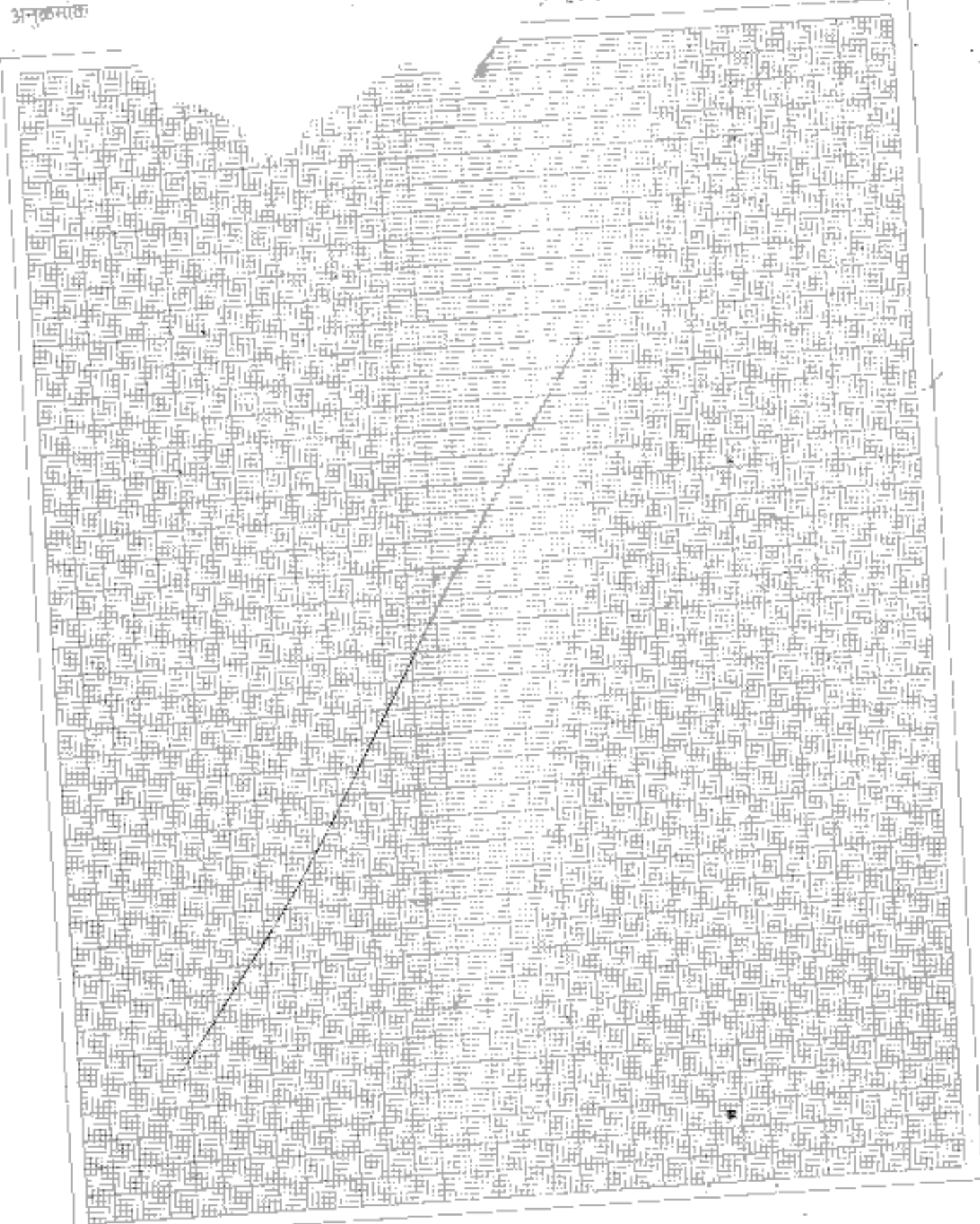
$$\text{Hence, area of shaded region} = \underline{\underline{42 \text{ cm}^2}}$$



Roll No

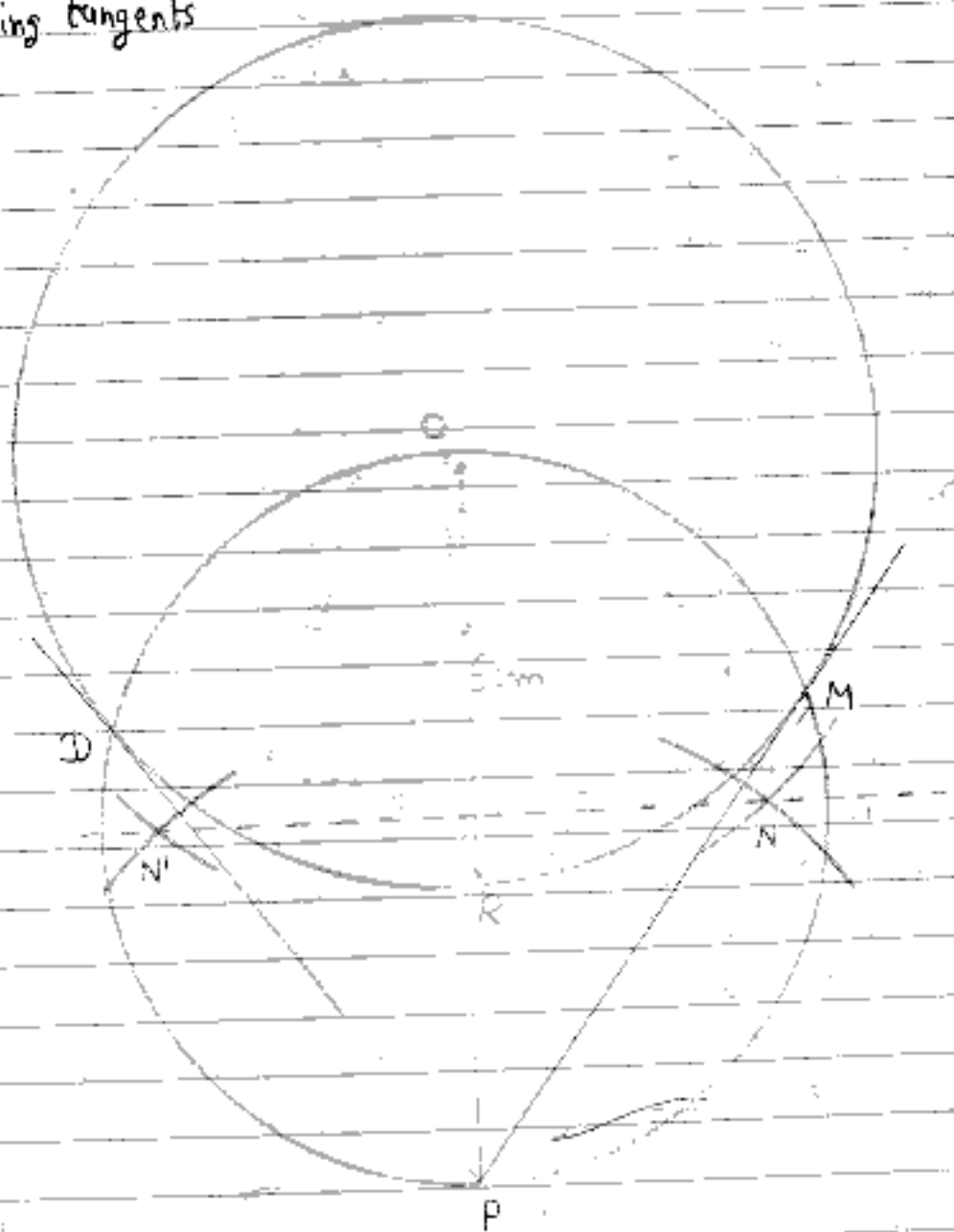
अनुक्रमणिका

25/24/2020



Qus. 24 Ans.

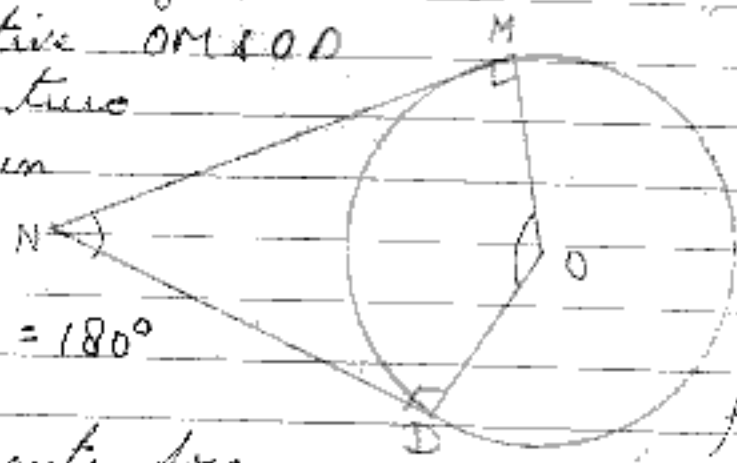
⇒ Drawing tangents



In provided fig. by construction  
we have, radius  $OR = 6\text{ cm}$   
line seg.  $OP = 10\text{ cm}$   
Therefore, we receive  
tangents  $PD$  &  $PM$   
such that :  $PD = 8\text{ cm}$   
 $PM = 8\text{ cm}$

## Qus. 25 Ans...

⇒ Let,  $O$  be centre of a circle  
its be respective  $OM$  &  $OD$   
&  $MN$  &  $DN$  are two  
tangents drawn  
to given circle.  $N$



To prove:  $\angle MND + \angle MOD = 180^\circ$

i.e. angle b/w tangents from  
external point to circle is supplementary  
to angle subtended by line-seg joining  
point of contact at centre.

Proof: It is clear from fig. that  $MODN$   
is a quadrilateral.

Sum of all interior angles in a quadrilateral  
=  $360^\circ$

$$\angle M + \angle O + \angle N + \angle D = 360^\circ \rightarrow \textcircled{1}$$

Also, we know,  $\angle M = \text{right angle} = 90^\circ$   
&  $\angle D = \text{right angle} = 90^\circ$

[ $\because$  because tangents radius drawn to  
point of contact form are perpendicular  
to tangents i.e. forms  $90^\circ$ ]

Putting these values in eq<sup>n</sup>  $\textcircled{1}$ ,  
we obtain:

$$\Rightarrow 90^\circ + \angle O + \angle N + 90^\circ = 360^\circ$$

$$\Rightarrow \angle O + \angle N = 360^\circ - 90 - 90$$

$$\Rightarrow \angle O + \angle N = 180^\circ$$

Hence, proved that  $\angle MNO$  and  $\angle MOD$  are supplementary!

### Qus. 26 Xiv...

$\Rightarrow$  Let the speed of stream be ' $x$  km/hr'  
Given  $\Rightarrow$  speed of boat 18 km/hr  
& distance = 24 km  
Case I: When <sup>boat</sup> speed goes upstream  
then its speed  $\Rightarrow (18-x)$  km/h

Also, Time =  $\frac{\text{Distance}}{\text{Speed}}$  [Let time taken be  $T_1$ ]

$$T_1 = \frac{24}{18-x}$$

Case II: When boat goes downstream  
its speed  $\Rightarrow (18+x)$  km/h  
Let, time taken be  $T_2$

$$\Rightarrow T_2 = \frac{24}{18+x}$$

According to question,  
more boat taken 1 hour more  
when it goes upstream than  
downstream.

This implies that ?

$$\Rightarrow \frac{24}{(18-x)} - \frac{24}{(18+x)} = 1 \quad \text{ie } T_1 - T_2 = 1$$

$$\Rightarrow \frac{24(18+x) - 24(18-x)}{(18-x)(18+x)} = 1 \quad \text{[}\because (a-b)(a+b) = a^2 - b^2\text{]}$$

$$\Rightarrow \frac{432 + 24x - 432 + 24x}{(18)^2 - (x)^2} = 1$$

To,

$$\Rightarrow 48x = 324 - x^2$$
$$x^2 + 48x - 324 = 0 \quad [ax^2 + bx + c] \text{ standard form}$$

Using quadratic formula

$$\frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$\frac{-48 \pm \sqrt{(48)^2 - 4(1)(-324)}}{2(1)}$$

$$\Rightarrow \frac{-48 \pm \sqrt{3600}}{2}$$

$$\Rightarrow \frac{-48 \pm 60}{2}$$

for (+ve)  $\frac{-48+60}{2} = \frac{12}{2} = \boxed{6} \text{ km/hr}$

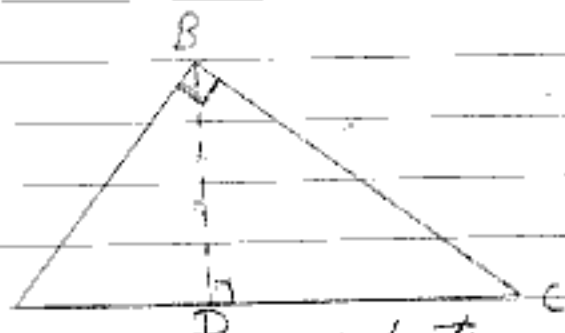
for (-ve)  $\frac{-48-60}{2} = \frac{-108}{2} = \boxed{-54}$

Since, speed is a measure, which can't be negative.

Therefore, speed of stream,  $x = \boxed{6 \text{ km/hr}}$

## Qus 28. Ans...

⇒ Let, ABC be a right  $\Delta$   
right angled at B



To prove:  $AC^2 = AB^2 + BC^2$   
i.e. square of hypotenuse is equal to  
sum of squares of other 2 sides.

Construction: Draw  $BD \perp AC$

Proof: We know, Theorem, that  
[∵ If a perpendicular is drawn from vertex  
of right angle in a right triangle to  
hypotenuse, then triangles formed  
on each side are similar to whole  
and to each other]

$$\Rightarrow \Delta ABD \sim \Delta ACB$$

Then, according to Thales theorem

$$\frac{AD}{AB} = \frac{AB}{AC}$$

$$\Rightarrow AC \cdot AD = AB^2 \rightarrow (1)$$

Also,  $\Delta BDC \sim \Delta ABC$  [from above used theorem]

Then, by Thales theorem:

$$\frac{CD}{BC} = \frac{BC}{AC}$$

$$\Rightarrow CD \cdot AC = BC^2 \rightarrow (2)$$

On adding eq<sup>n</sup> (1) & (2), we obtain

$$AB^2 + BC^2 = AC \cdot AD + AC \cdot CD$$

$$\Rightarrow AB^2 + BC^2 = AC(AD + CD)$$

from fig, we have  $AD + CD = AC$

Therefore,  $AB^2 + BC^2 = AC(AC)$

To  $AB^2 + BC^2 = AC^2$

Hence, proved! i.e.  $AC^2 = AB^2 + BC^2$

∴ In a right  $\Delta$ , sq. of hypotenuse  
= sum of sq.s of other 2 sides

### Qus. 29 Ans....

⇒ Given, a pipe of diameter = 2.0 cm

Then, area of its cross-section  
=  $\pi r^2 = \pi \left(\frac{0.2}{2}\right)^2$

Also, given, a rate of flow of water = 3 km/hr

or  $\Rightarrow \frac{3000 \text{ m}}{60 \text{ min}} = 50 \text{ m/min}$

Thus, we can conclude that total water  
discharge from pipe in a min

⇒ area of cross section  $\times$  speed

$$\Rightarrow \pi (0.1)^2 \times 50 \quad \Rightarrow \pi \times 0.01 \times 50$$

$$\Rightarrow \underline{0.5 \pi \text{ cm}^2}$$

To find time in which tank will be filled;

Let, time taken be 'T'

Given, cylindrical tank : diameter = 10 cm

ht. (depth) = 2 cm

Then, total water in it = its volume

$$\Rightarrow \pi r^2 h = \pi \left(\frac{10}{2}\right)^2 \times 2 = \pi (5)^2 \times 2$$

Arithmetically, time (T) in which tank will be filled with water by pipe

$$\Rightarrow \pi \times T \times 0.5 \pi$$

$$\Rightarrow T \cdot 0.5 \pi = \pi (5)^2 \times 2$$

$$T = \frac{\pi (5)^2 \times 2}{0.5 \pi} = \frac{5^2 \times 2}{0.5} = \frac{50}{0.5} = \boxed{100} \text{ Min}$$

Thus, in 100 minutes tank will be filled by water. (using pipe) !!



## Qus. 30 Ans...

C. I. (Marks)	0-10	10-20	20-30	30-40	40-50	50-60
No. of students	6	14	10	15	5	10

To find mode:

It is clear from given data that, highest frequency i.e. 15 belong to class interval 30-40.

Hence, C.I.: 30-40  $\Rightarrow$  class Modal Class

Now,

Lower limit of modal class,  $l = 30$

Frequency of modal class,  $f_1 = 15$

Frequency of class preceding modal class,  $f_0 = 10$

Frequency of class succeeding modal class,  $f_2 = 5$

Difference b/w upper & lower limit of modal class, i.e.  $40 - 30$ ,  $h = 10$

Now, we know:

$$\text{Mode} = l + \left[ \frac{f_1 - f_0}{2f_1 - f_0 - f_2} \right] \times h$$

Substituting <sup>required</sup> values in provided formula we obtain;

$$\Rightarrow 30 + \left[ \frac{15 - 10}{2(15) - 10 - 5} \right] \times 10$$

$$\Rightarrow 30 + \left[ \frac{5}{30 - 10 - 5} \right] \times 10$$

$$\Rightarrow 30 + \frac{5}{15} \times 10$$

$$\Rightarrow 30 + \frac{1 \times 10}{3}$$

$$\Rightarrow 30 + 3.33$$

$$\Rightarrow \boxed{33.33} \text{ Ans}$$

Hence, modes of marks obtained =  $\boxed{33.33}$

### Ques. 27 Ans...

$\Rightarrow$  Given two poles of equal ht.

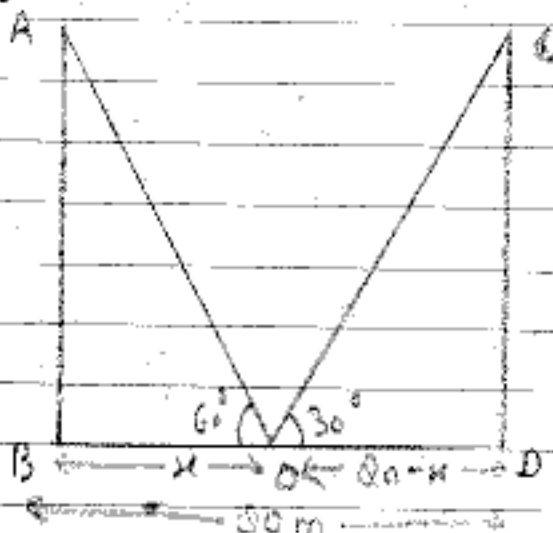
let  $AB = CD$

Distance b/w two poles = 80m

& O is point of BD

Let,  $BO = x$  metre

$DO = 80 - x$  metre.



Also given, respective angle of elevation b/w them.

Now, from fig.

$$\text{In } \triangle ABO, \tan 60^\circ = \frac{AB}{BO}$$

$$\Rightarrow \sqrt{3} = \frac{AB}{x} \Rightarrow x = \frac{AB}{\sqrt{3}} \text{ or } BO = \frac{AB}{\sqrt{3}} \quad \text{--- (1)}$$

$$\text{In } \triangle COD, \tan 30^\circ = \frac{CD}{DO}$$

$$\Rightarrow \frac{1}{\sqrt{3}} = \frac{CD}{80-x} \Rightarrow 80-x = CD\sqrt{3} \text{ or } DO = CD\sqrt{3} \quad \text{--- (2)}$$

$$\text{We know, } BO + DO = 80$$

$\Rightarrow$  from eq (1) & (2) we substitute value of  $BO$  &  $DO$

$$\Rightarrow \frac{AB}{\sqrt{3}} + CD\sqrt{3} = 80$$

$$\Rightarrow \frac{AB + CD\sqrt{3}(\sqrt{3})}{\sqrt{3}} = 80$$

$$\Rightarrow AB + 3CD = 80\sqrt{3}$$

$$\Rightarrow 4AB = 80\sqrt{3}$$

$$AB = \frac{80\sqrt{3}}{4} = 20\sqrt{3} \quad [\because AB = CD \text{ given}]$$

Hence ht. of ~~each~~ <sup>each</sup> poles =  $20\sqrt{3}$  m

$$\text{Now, we know, } x = \frac{AB}{\sqrt{3}} = \frac{20\sqrt{3}}{\sqrt{3}} = 20$$

We get, ~~at~~  $x = 20$  m =  $BO$

Also,  $DO = 80 - x$

$$DO = 80 - 20 = \underline{60 \text{ m}}$$

Hence, height of each pole =  $20\sqrt{3} \text{ m}$

distance of  $BO = 20 \text{ m}$

" "  $DO = 60 \text{ m}$

Answer